

**ANIL NEERUKONDA INSTITUTE OF TECHNOLOGY & SCIENCES
(AUTONOMOUS)**

M.Tech II-Semester Regular Examinations, May 2016

**Statistical signal processing
(Communication Systems)**

Date:

Time: 3 hours

Max Marks: 60

Answer ONE Question from each unit

All questions carry equal marks

All parts of the question must be answered at one place only

UNIT-I

1) Explain in detail about the role of estimation in signal processing? Write about the Cramer-Rao Lower bound. [12M]

(OR)

2) Write about unbiased estimators. Write about finding MVU estimators. [12M]

UNIT-II

3) Write about recursive least squares estimation. [12M]

(OR)

4) Explain the best linear unbiased estimation. [12M]

UNIT-III

5) Explain the Bayesian Linear model. [12M]

(OR)

6) Explain about maximum a posteriori estimators. [12M]

UNIT-IV

7) a) What is a dynamical system ? [2M]

b) Define the state of a dynamical system? [2M]

c) Distinguish between Weiner and Kalman filters? [4M]

d) What is meant by 'innovation' w.r.t. the Kalman filter ? [2M]

e) What is the Extended Kalman Filter (EKF) ? [2M]

(OR)

- 8) Assume we observe the data $x[k] = Ar^k + w[k]$ for $k = 0, 1, \dots, N$; where A is the realization of a random variable with p.d.f. $N(\mu_A, \sigma_A^2)$, $0 < r < 1$, and the $w[k]$'s are samples of WGN, with variance σ^2 . Also assume that A is independent of the $w[k]$'s. Find the sequential MMSE estimator of A based on $\{x[0], x[1], \dots, x[N]\}$. **[12M]**

UNIT-V

- 9) a) Derive the likelihood ratio test (LRT), under the Neyman Pearson (NP) criterion for a binary hypothesis problem. **[8M]**
- b) When does the LRT test under minimum probability of error criterion become identical to that under NP criterion? **[4M]**

(OR)

- 10) a) Consider the following detection problem: Under hypothesis H_0 , the measured data is $x[0] = w[0]$; where $w[0]$ is zero mean Gaussian noise with variance 1. Under hypothesis H_1 , $x[0] = 2 + w[0]$. A detector decides H_1 if $x[0] > 1$ and H_0 otherwise. What is the probability of false alarm in this case. **[6M]**
- b) Under what criteria is the detector optimal? Explain? **[6M]**
